

**On-line Table 1: Patient and aneurysm characteristics**

| Patients |     |      |       | Aneurysms (n = 65) |      |      |      |      |          |     |
|----------|-----|------|-------|--------------------|------|------|------|------|----------|-----|
| Sex      | No. | Age  | Years | Variable           | Mean | SD   | Min  | Max  | Location | No. |
| Female   | 36  | Mean | 54.6  | Max size           | 8.56 | 3.56 | 2.19 | 20.4 | MCA      | 41  |
| Male     | 14  | SD   | 10.2  | Neck size          | 5.80 | 2.48 | 1.28 | 14.2 | ICA      | 10  |
| Unknown  | 7   | Min  | 30    | Aspect ratio       | 1.11 | 0.59 | 0.16 | 3.73 | AcomA    | 8   |
| Total    | 57  | Max  | 77    | Size ratio         | 1.56 | 0.55 | 0.96 | 3.94 | PcomA    | 4   |
|          |     |      |       |                    |      |      |      |      | PICA     | 2   |

**Note:**—AcomA indicates anterior communicating artery; PcomA, posterior communicating artery.

**On-line Table 2: Hemodynamic variables studied on each aneurysm wall region**

| Variable | Definition                                                                                                          | Measure                                                                                                          |
|----------|---------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------|
| PRE      | $\bar{p} = \frac{1}{T} \int_0^T p \, dt$                                                                            | Provides an indication of flow impingement where the pressure is higher                                          |
| WSS      | $\bar{\tau} = \frac{1}{T} \int_0^T  \tau  \, dt$                                                                    | Measures the average magnitude of the viscous forces of the blood flow on the vascular wall                      |
| OSI      | $OSI = \frac{1}{2} \left( 1 - \left  \frac{\int_0^T \tau \, dt}{\int_0^T  \tau  \, dt} \right  \right)$             | Measures the degree of directional oscillation of the WSS vector during the cardiac cycle                        |
| RRT      | $RRT = \frac{1}{(1 - 2 \times OSI) \times \bar{\tau}}$                                                              | Measures, on average, how slow the flow is near the vascular wall                                                |
| WSSGRD   | $\mathbf{G} = \nabla  \tau $<br>$G =  \mathbf{G} $                                                                  | Measures the average magnitude of the wall shear stress gradient (variations of wall shear stress magnitude)     |
| WSSDIV   | $D = \nabla \times \mathbf{G}$                                                                                      | Measures the average degree of convergence/divergence of WSS vectors                                             |
| GON      | $GON = \frac{1}{2} \left( 1 - \left  \frac{\int_0^T \mathbf{G} \, dt}{\int_0^T  \mathbf{G}  \, dt} \right  \right)$ | Measures the degree of directional oscillation of the wall shear stress gradient vector during the cardiac cycle |

**Note:**—GON indicates gradient oscillatory number;  $p$ , the instantaneous pressure;  $\tau$ , the instantaneous wall shear stress vector;  $T$ , the period of the cardiac cycle.

On-line Table 3: Summary of hemodynamic variables over the 5 aneurysm wall regions and the entire aneurysm sac<sup>a</sup>

| Variable  | A (n = 32)                     | H (n = 61)                      | T (n = 78)                      | R (n = 13)                      | N (n = 61)                      | P                  | Whole Sac (n = 61)              |
|-----------|--------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|--------------------|---------------------------------|
| OSImax    | 0.087 (0.026–0.253)            | 0.086 (0.021–0.275)             | 0.031 (0.006–0.099)             | 0.117 (0.037–0.223)             | 0.27 (0.187–0.363)              | <.001 <sup>b</sup> | 0.33 (0.237–0.405)              |
| OSIavg    | 0.012 (0.005–0.032)            | 0.011 (0.004–0.022)             | 0.006 (0.002–0.012)             | 0.012 (0.008–0.019)             | 0.013 (0.006–0.02)              | <.001 <sup>b</sup> | 0.013 (0.009–0.021)             |
| OSImin    | 0.001 (0–0.003)                | 0.00 (0–0.000)                  | 0.00 (0–0.000)                  | 0.001 (0–0.001)                 | 0.00 (0–0)                      | <.001 <sup>b</sup> | 0.00 (0–0)                      |
| WSSmax    | 20.247 (6.204–50.168)          | 36.673 (19.121–51.04)           | 28.067 (10.037–52)              | 20.219 (4.51–33.722)            | 76.33 (34.469–107.27)           | <.001 <sup>b</sup> | 84.071 (48.316–137.99)          |
| WSSavg    | 6.472 (2.419–20.753)           | 9.7 (5.299–22.681)              | 13.813 (4.431–27.974)           | 3.502 (2.533–13.449)            | 12.182 (5.774–20.872)           | .09                | 11.978 (5.401–21.031)           |
| WSSmin    | 0.823 (0.483–3.53)             | 1.479 (0.599–5.57)              | 3.4 (1.182–9.626)               | 1.665 (0.471–1.795)             | 0.571 (0.203–1.402)             | <.001 <sup>b</sup> | 0.314 (0.12–0.795)              |
| PREmax    | 1998.33 (1575.22–4350.99)      | 2154.95 (1395.49–4450.29)       | 1949.34 (951.176–4277.51)       | 1467.8 (1104.85–5276.45)        | 2157.87 (1161.31–6060.67)       | .86                | 2157.87 (1246.98–6060.67)       |
| PREavg    | 1908.01 (1563.66–4254.1)       | 2077.32 (1343.62–4357.96)       | 1874.47 (938.024–4205.03)       | 1371.74 (1048.57–4640.82)       | 1936.72 (1049.65–4378.17)       | .88                | 1929.39 (1046.39–4405.53)       |
| PREmin    | 1854.5 (1555.44–4046.99)       | 1906.65 (1264.43–4130.58)       | 1737.71 (908.966–4126.97)       | 1315.31 (1017.11–4379.42)       | 1698.72 (846.361–3705.44)       | .71                | 1467.21 (825.304–3550.19)       |
| RRTmax    | 1.643 (0.726–5.102)            | 0.835 (0.186–4.187)             | 0.329 (0.117–1.136)             | 1.182 (0.626–2.494)             | 3.833 (0.91–19.093)             | <.001 <sup>b</sup> | 8.381 (2.497–25.156)            |
| RRTavg    | 0.395 (0.093–0.652)            | 0.204 (0.064–0.402)             | 0.109 (0.045–0.253)             | 0.386 (0.13–0.977)              | 0.211 (0.095–0.542)             | .003 <sup>b</sup>  | 0.231 (0.107–0.812)             |
| RRTmin    | 0.051 (0.02–0.169)             | 0.028 (0.02–0.053)              | 0.036 (0.02–0.1)                | 0.05 (0.03–0.226)               | 0.013 (0.009–0.03)              | <.001 <sup>b</sup> | 0.012 (0.007–0.021)             |
| GONmax    | 0.562 (0.379–0.709)            | 0.601 (0.425–0.758)             | 0.41 (0.263–0.579)              | 0.588 (0.525–0.666)             | 0.793 (0.677–0.871)             | <.001 <sup>b</sup> | 0.84 (0.723–0.892)              |
| GONavg    | 0.05 (0.025–0.101)             | 0.06 (0.038–0.091)              | 0.041 (0.019–0.065)             | 0.06 (0.035–0.088)              | 0.062 (0.047–0.083)             | <.001 <sup>b</sup> | 0.06 (0.053–0.089)              |
| GONmin    | 0.00 (0–0.001)                 | 0.00 (0–0.000)                  | 0.00 (0–0.000)                  | 0.00 (0–0.001)                  | 0.00 (0–0)                      | <.001 <sup>b</sup> | 0.00 (0–0)                      |
| WSSDIVmax | 797.149 (117.648–2347.34)      | 972.411 (366.794–1873.63)       | 796.119 (41.758–1793.64)        | 173.792 (59.715–936.614)        | 3389.54 (1577.48–8564.27)       | <.001 <sup>b</sup> | 6298.13 (3389.54–11916)         |
| WSSDIVavg | 9.405 (–41.012–83.128)         | 3.361 (–80.042–56.757)          | 8.961 (–67.936–184.01)          | –3.287 (–53.965–82.407)         | 6.216 (–36.183–49.359)          | .75                | 25.498 (6.323–45.645)           |
| WSSDIVmin | –673.202 (–1465.48 to –83.799) | –873.752 (–1433.32 to –355.594) | –629.641 (–1474.23 to –242.559) | –364.995 (–609.969 to –156.414) | –2164.16 (–4212.58 to –748.606) | <.001 <sup>b</sup> | –2942.55 (–5636.66 to –1204.95) |
| WSSGRDmax | 1016.65 (166.46–1940.3)        | 1385.98 (596.903–2165.81)       | 953.849 (366.306–2139.57)       | 525.83 (177.07–1095.26)         | 3442.6 (1414.75–6410.17)        | <.001 <sup>b</sup> | 5215.49 (2566.13–8098.6)        |
| WSSGRDavg | 273.177 (59.423–538.36)        | 268.379 (127.283–455.09)        | 359.303 (136.56–646.408)        | 116.625 (64.414–290.717)        | 313.57 (148.346–537.11)         | .23                | 295.205 (144.333–545.926)       |
| WSSGRDmin | 15.023 (4.158–41.35)           | 23.1 (4.791–52.966)             | 45.416 (15.871–87.563)          | 10.857 (4.065–38.541)           | 7.213 (2.612–19.299)            | <.001 <sup>b</sup> | 4.666 (1.501–14.244)            |
| WSSNorm   | 0.242 (0.079–0.641)            | 0.271 (0.15–0.549)              | 0.428 (0.203–0.785)             | 0.141 (0.06–0.393)              | 0.322 (0.2–0.616)               | .04 <sup>b</sup>   | 0.308 (0.186–0.585)             |

**Note:**—K-W indicates Kruskal-Wallis; norm, normal; A, atherosclerotic; H, hyperplastic; T, thin; R, ruptured; N, normal-appearing; WSSDIV, WSS divergence; WSSGRD, WSS stress gradient.

<sup>a</sup> Values of median and lower and upper quartiles are given. The number of regions of each type in the headers is indicated in parentheses. *P* values correspond to the K-W test.

<sup>b</sup> Significant.

**On-line Table 4: Multivariate model of atherosclerotic and hyperplastic versus normal regions<sup>a</sup>**

| Variable       | Coefficient | Frequency | Std Coeff | OR (95% CI)                        |
|----------------|-------------|-----------|-----------|------------------------------------|
| GONmin         | 88.80773    | 1         | 2.52083   | 3.7043e + 38 (14.66–2.47669e + 56) |
| RRTavg         | 2.01944     | 1         | 1.88564   | 7.53 (1.47–8.46)                   |
| WSSGRDmax      | −0.05881    | 1         | −1.72039  | 0.94 (0.92–0.99)                   |
| OSImax         | −0.12794    | 1         | −1.54099  | 0.88 (0.87–0.95)                   |
| OSImin         | −7.29386    | 0.542     | −1.20267  | 0 (0–1)                            |
| OSIavg         | 0.76674     | 1         | 0.88435   | 2.15 (1.03–3.05)                   |
| WSSGRDmin      | 3.98366     | 1         | 0.77905   | 53.71 (3.19–85.41)                 |
| WSSmax         | 0.04052     | 0.186     | 0.64801   | 1.04 (1–1.13)                      |
| PREavg         | −18.8527    | 1         | −0.57273  | 0 (0–0.01)                         |
| WSSmin         | 1.69471     | 1         | 0.43032   | 5.45 (1.6–12.13)                   |
| RRTmax         | −0.00509    | 0.971     | −0.404    | 0.99 (0.99–1)                      |
| GONavg         | −0.46981    | 0.36      | −0.24288  | 0.63 (0.41–1)                      |
| RRTmin         | 0.5952      | 0.558     | 0.21015   | 1.81 (1–3.21)                      |
| WSSGRDavg      | −0.15048    | 0.186     | −0.18058  | 0.86 (0.68–1)                      |
| PREmin         | 1.51198     | 1         | 0.1632    | 4.54 (1.75–4.94)                   |
| WSSDIVmax      | 0.00035     | 0.712     | 0.14986   | 1 (1–1)                            |
| WSSavg         | 0.13314     | 0.542     | 0.12466   | 1.14 (1–1.18)                      |
| GONmax         | −0.01021    | 0.915     | −0.04779  | 0.99 (0.97–1)                      |
| WSSDIVmin      | 0.00014     | 0.186     | 0.03344   | 1 (1–1)                            |
| PREmax         | −0.05266    | 0.523     | −0.0109   | 0.95 (0.69–1)                      |
| WSSDIVavg      | 0           | 0.091     | 0         | 1 (1–1)                            |
| Intercept      | 17.14893    | —         | —         | —                                  |
| Regularization |             |           | 0.002     |                                    |
| AUC            |             |           | 0.9214    |                                    |

**Note:**—AUC indicates area under the receiver operating characteristic curve; Std Coeff, standardized coefficients; OR, odds ratio, CI, confidence intervals; WSSDIV, WSS divergence; WSSGRD, WSS stress gradient.

<sup>a</sup> The model variables are ordered by their influence on the outcome—that is, by the magnitude of the standardized coefficients. “Frequency” indicates the percentage of times the variable was retained in the cross-validation step.

**On-line Table 5: Multivariate model of thin-versus-normal regions<sup>a</sup>**

| Variable       | Coefficient | Frequency | Std Coeff | OR (95% CI)             |
|----------------|-------------|-----------|-----------|-------------------------|
| WSSGRDmin      | 10.60181    | 1         | 2.222     | 40207.4 (18.96–46534.3) |
| WSSGRDmax      | −0.06647    | 0.999     | −2.03258  | 0.94 (0.88–0.99)        |
| GONavg         | −1.87558    | 0.981     | −1.15092  | 0.15 (0.09–0.93)        |
| RRTmin         | 4.35777     | 1         | 1.08302   | 78.08 (21.97–111.22)    |
| RRTmax         | −0.01476    | 1         | −0.89416  | 0.99 (0.98–0.99)        |
| PREmax         | −4.29996    | 1         | −0.81946  | 0.01 (0–0.38)           |
| GONmax         | −0.16194    | 1         | −0.74147  | 0.85 (0.83–0.85)        |
| OSIavg         | 0.68091     | 0.981     | 0.51464   | 1.98 (1.02–2.07)        |
| PREmin         | 2.92509     | 0.997     | 0.37532   | 18.64 (1.24–19.3)       |
| WSSDIVavg      | 0.02076     | 0.931     | 0.373     | 1.02 (1–1.04)           |
| OSImin         | 1.71287     | 0.86      | 0.31894   | 5.54 (0.58–13.47)       |
| WSSGRDavg      | 0.12232     | 0.61      | 0.2182    | 1.13 (1–5.1)            |
| GONmin         | 1.17317     | 0.677     | 0.2113    | 3.23 (1–1.66303e + 31)  |
| OSImax         | −0.01405    | 0.995     | −0.17754  | 0.99 (0.98–1)           |
| WSSDIVmin      | 0.00028     | 0.64      | 0.0671    | 1 (1–1)                 |
| WSSmax         | −0.00168    | 0.507     | −0.02824  | 1 (0.83–1)              |
| PREavg         | 0           | 0.425     | 0         | 1 (1–1.32078e + 07)     |
| WSSavg         | 0           | 0.021     | 0         | 1 (1–1)                 |
| WSSmin         | 0           | 0.062     | 0         | 1 (1–1.54)              |
| RRTavg         | 0           | 0.224     | 0         | 1 (1–1.34)              |
| WSSDIVmax      | 0           | 0.317     | 0         | 1 (1–1)                 |
| Intercept      | 3.83878     | —         | —         | —                       |
| Regularization |             |           | 0.004     |                         |
| AUC            |             |           | 0.9666    |                         |

**Note:**—AUC indicates area under the receiver operating characteristic curve; Std Coeff, standardized coefficients; WSSDIV, WSS divergence; WSSGRD, WSS stress gradient.

<sup>a</sup> The model variables are ordered by their influence on the outcome—that is, by the magnitude of the standardized coefficients. “Frequency” indicates the percentage of times the variable was retained in the cross-validation step.

**On-line Table 6: Multivariate model of atherosclerotic and hyperplastic versus thin regions<sup>a</sup>**

| Variable       | Coefficient | Frequency | Std Coeff | OR (95% CI)      |
|----------------|-------------|-----------|-----------|------------------|
| RRTavg         | 0.25935     | 1         | 0.25919   | 1.3 (1.42–1.87)  |
| GONmax         | 0.05254     | 1         | 0.22511   | 1.05 (1.06–1.13) |
| WSSmin         | −0.02742    | 0.996     | −0.02742  | 0.98 (0.17–0.9)  |
| RRTmax         | 0.00366     | 0.992     | 0.00366   | 1 (1–1.03)       |
| GONavg         | 0           | 0.961     | 0         | 1 (1–2.33)       |
| GONmin         | 0           | 0.984     | 0         | 1 (0.01–0.7)     |
| PREavg         | 0           | 0.631     | 0         | 1 (0.05–1)       |
| PREmax         | 0           | 0.942     | 0         | 1 (1–13.62)      |
| PREmin         | 0           | 0.845     | 0         | 1 (0.53–1)       |
| WSSavg         | 0           | 0.25      | 0         | 1 (0.71–1)       |
| WSSmax         | 0           | 0.979     | 0         | 1 (1.02–1.58)    |
| OSlavg         | 0           | 0.002     | 0         | 1 (1–1)          |
| OSlmax         | 0           | 0.951     | 0         | 1 (0.92–1)       |
| OSlmin         | 0           | 0.977     | 0         | 1 (0.48–0.94)    |
| RRTmin         | 0           | 0.149     | 0         | 1 (1–1.24)       |
| WSSDIVavg      | 0           | 0.953     | 0         | 1 (0.97–1)       |
| WSSDIVmax      | 0           | 0.984     | 0         | 1 (1–1.01)       |
| WSSDIVmin      | 0           | 0.953     | 0         | 1 (1–1.01)       |
| WSSGRDavg      | 0           | 0.156     | 0         | 1 (0.99–1)       |
| WSSGRDmax      | 0           | 0.946     | 0         | 1 (0.8–1)        |
| WSSGRDmin      | 0           | 0.946     | 0         | 1 (1–16.84)      |
| Intercept      | −0.02742    | —         | —         | —                |
| Regularization |             |           | 0.00366   |                  |
| AUC            |             |           | 0.6953    |                  |

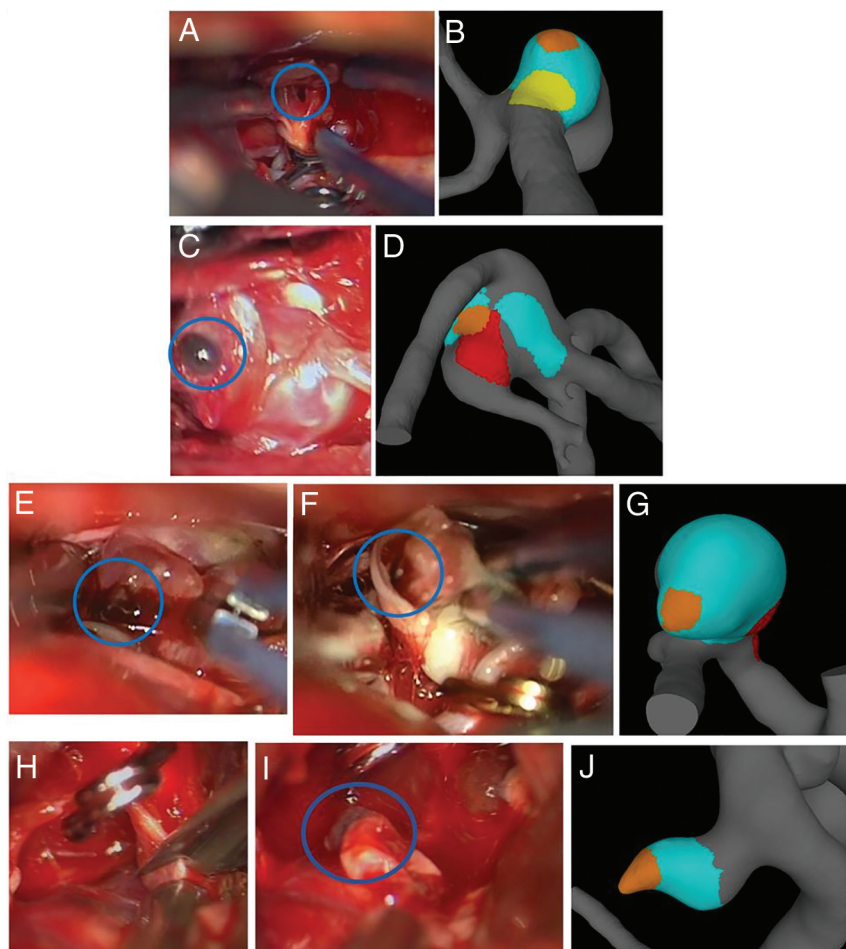
**Note:**—AUC indicates area under the receiver operating characteristic curve; Std Coeff, standardized coefficients; WSSDIV, WSS divergence; WSSGRD, WSS stress gradient.

<sup>a</sup> The model variables are ordered by their influence on the outcome—that is, by the magnitude of the standardized coefficients. “Frequency” indicates the percentage of times the variable was retained in the cross-validation step.

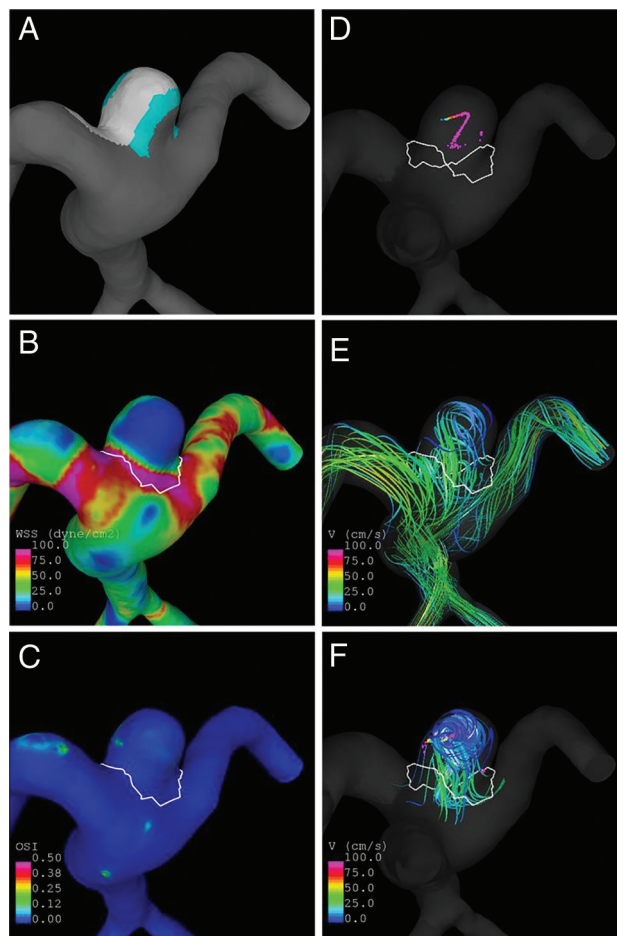
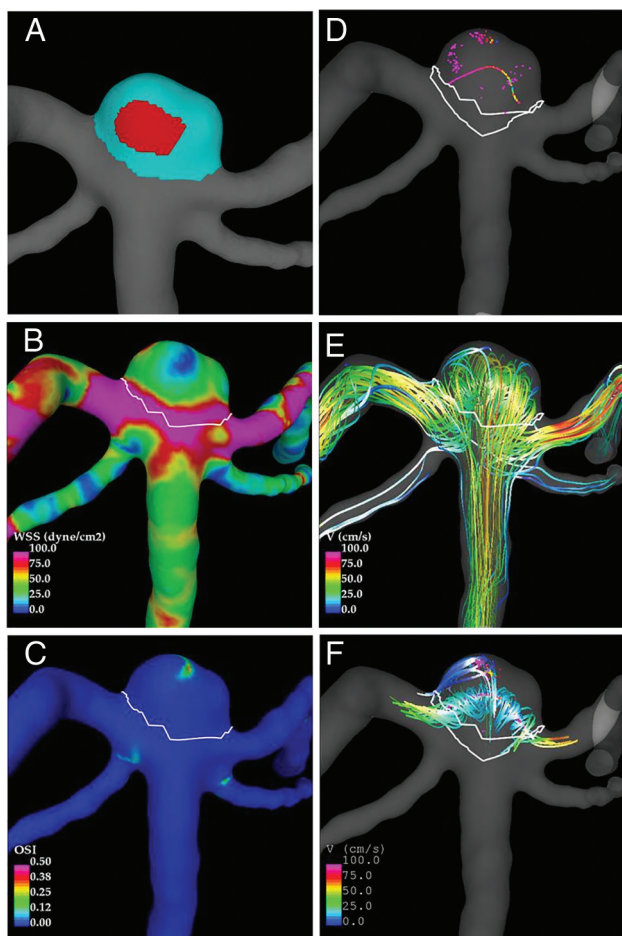
**On-line Table 7: Summary of results obtained from prior studies comparing computational fluid dynamics models with the visual appearance of the aneurysm wall during an operation**

| Study                                                                 | Data                                                                          | Findings                                                     |                                             |                                                                       | Comparison                                                                 |
|-----------------------------------------------------------------------|-------------------------------------------------------------------------------|--------------------------------------------------------------|---------------------------------------------|-----------------------------------------------------------------------|----------------------------------------------------------------------------|
|                                                                       |                                                                               | Rupture Site                                                 | Thin Wall                                   | Atherosclerotic Wall                                                  |                                                                            |
| Omodaka et al, 2012 <sup>28</sup>                                     | 6 MCAs (6 R)                                                                  | Lower WSS impingement (if bleb removed $\geq$ increased WSS) | —                                           | —                                                                     | Rupture point vs aneurysm region                                           |
| Fukazawa et al, 2015 <sup>29</sup>                                    | 12 MCAs (12 R)                                                                | Lower WSS                                                    | —                                           | —                                                                     | Pointwise (rupture vs dome + parent artery)                                |
| Sugiyama et al, 2013 <sup>30</sup><br>Kadasi et al, 2013 <sup>9</sup> | 30 MCAs (30 U)<br>16 IAs (4 AcomAs + 12 MCAs) (16 U)                          | —<br>—                                                       | —<br>Lower WSS and WSSG, higher PRE         | Prolonged RRT (also male sex)<br>—                                    | Regional<br>Point cloud comparison (thin vs normal + neck + parent artery) |
| Sugiyama et al, 2016 <sup>31</sup>                                    | 3 Patients with multiple IAs (3 atherosclerotic MCAs + 3 MCAs + 2 ICAs) (8 U) | —                                                            | —                                           | Lower WSS, prolonged RRT, inflow lower than in nonatherosclerotic IAs | Pointwise                                                                  |
| Talari et al, 2016 <sup>32</sup>                                      | 9 IAs (2 AcomAs + 2 PcomAs + 4 ICAs + 1 MCA) (9 U)                            | —                                                            | Higher PRE                                  | —                                                                     | Global features; no regional or pointwise comparison                       |
| Furukawa et al, 2018 <sup>33</sup>                                    | 24 IAs (13 MCAs + 9 ICAs + 2 ACAs) (10 R + 14 U)                              | —                                                            | —                                           | Lower WSS and AFI, higher OSI and RRT                                 | Pointwise comparison of hyperplastic vs thin                               |
| Cebral et al, 2018, this study                                        | 65 IAs (41 MCAs + 10 ICAs + 8 AcomAs + 4 PcomAs + 2 PICAs) (13 R + 52 U)      | Lower WSS, higher PRE                                        | Lower RRT, OSI, and GON; higher WSS and PRE | Lower WSS and PRE, prolonged RRT                                      | Regional, normalized                                                       |

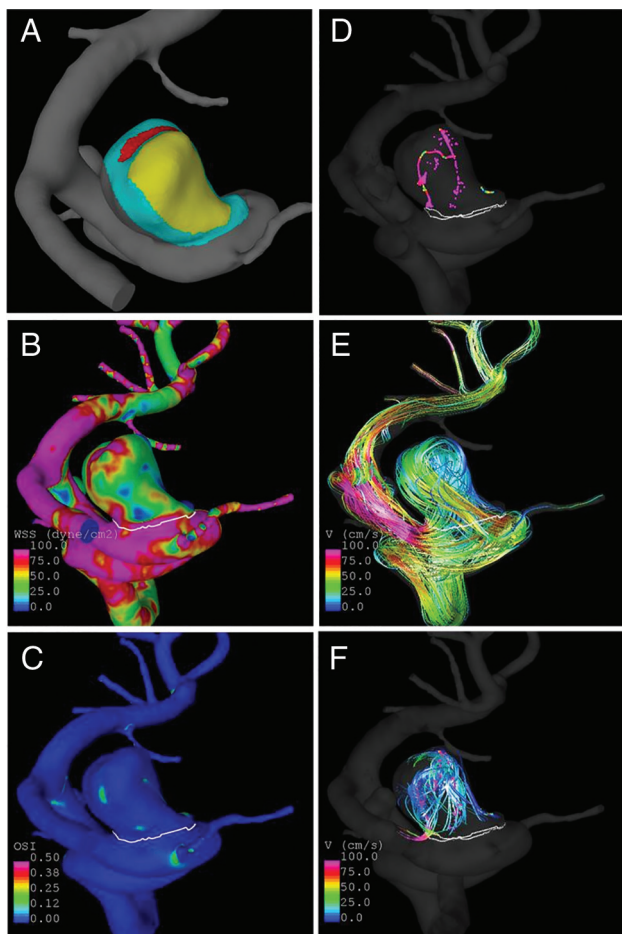
**Note:**—U indicates unruptured; AFI, aneurysm formation index; ACA, anterior cerebral artery; WSSG, wall shear stress gradient; AcomA, anterior communicating artery; PcomA, posterior communicating artery; R, ruptured.



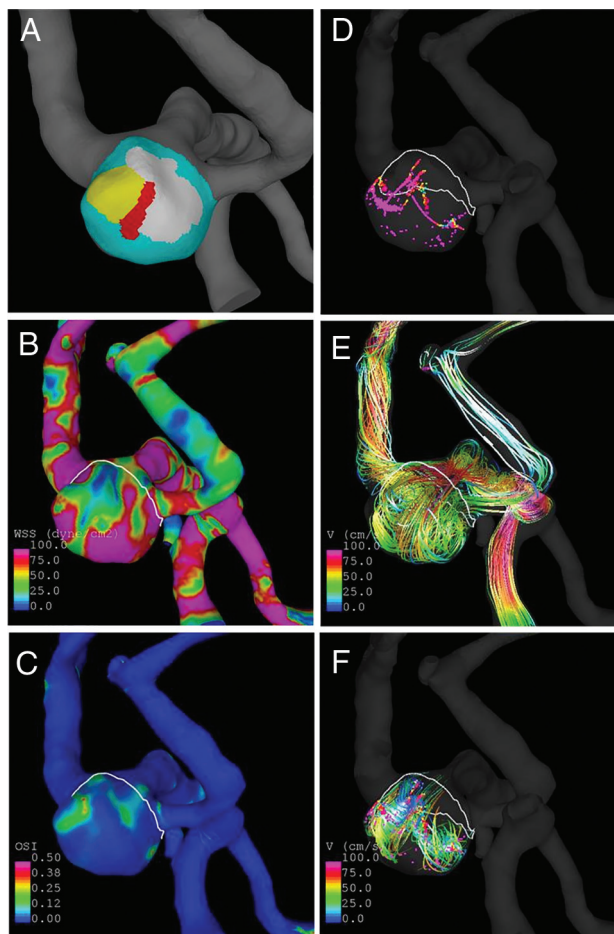
**ON-LINE FIG 1.** Identification of rupture site. Sample 1: *A*, Hole clearly observed on the side of the aneurysm. *B*, Rupture site marked in gold on the 3D model (views not matched). Sample 2: *C*, Mural hematoma corresponding to the rupture site at the distal end of the fundus. *D*, Rupture site in marked in gold. Sample 3: *E*, Small hematoma observed on aneurysm wall. *F*, Once the hematoma is removed, there is a hole in the aneurysm wall. *G*, Rupture site marked in in gold. Sample 4: *H*, Dome of ruptured aneurysm resected after ligation. *I*, Mural hematoma observed at the distal end of the resected dome. *J*, Rupture site marked in in gold.





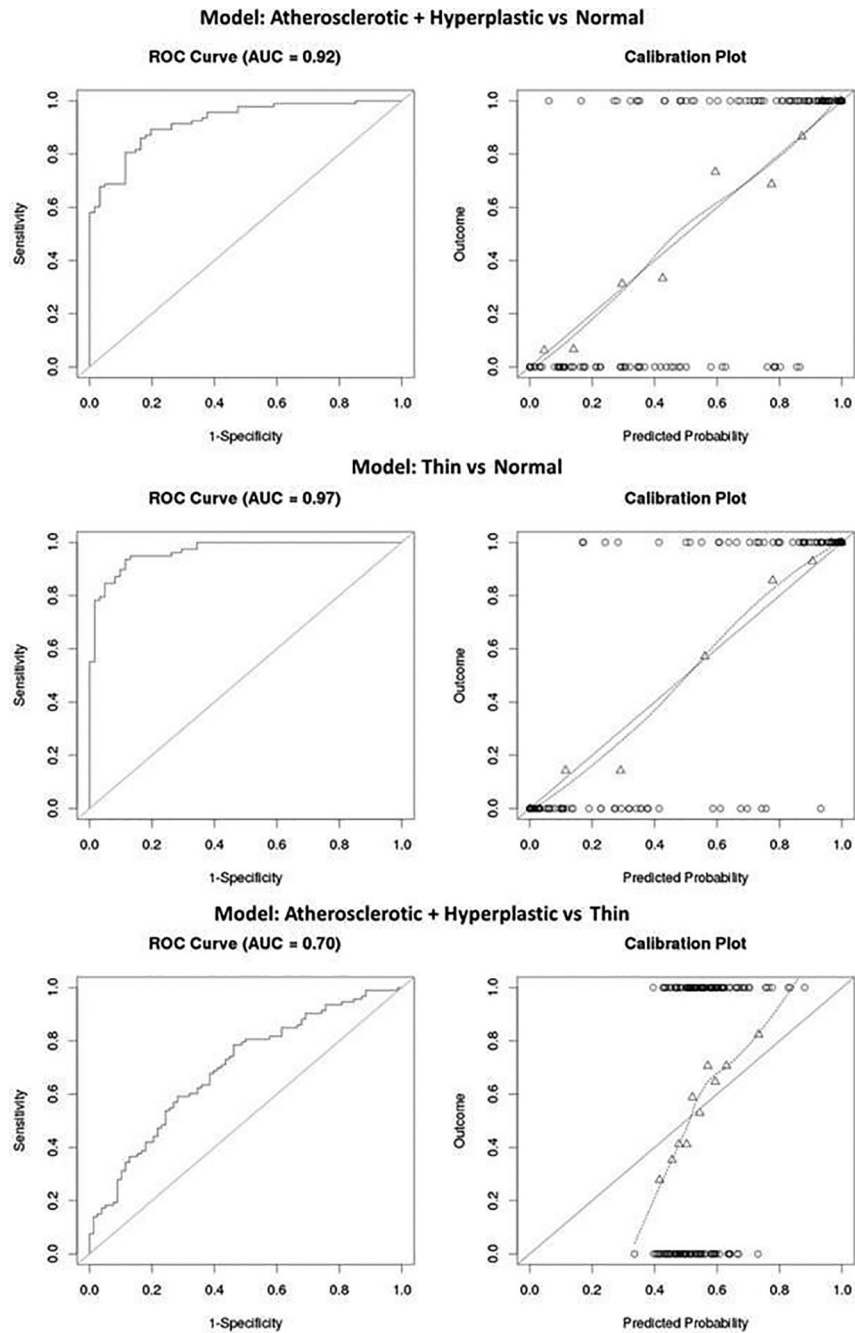


**ON-LINE FIG 4.** Sample aneurysm with thin and atherosclerotic regions. A, Wall regions (red indicates thin; yellow, atherosclerotic; cyan, normal-appearing). B, Wall shear stress. C, Oscillatory shear index. D, Vortex core lines. E, Flow streamlines. F, Swirling around vortex core lines.



**ON-LINE FIG 5.** Sample aneurysm with thin, hyperplastic, and atherosclerotic regions. A, Wall regions (red indicates thin; yellow, atherosclerotic; white, hyperplastic; cyan, normal-appearing). B, Wall shear stress. C, Oscillatory shear index. D, Vortex core lines. E, Flow streamlines. F, Swirling around the vortex core lines.





**ON-LINE FIG 6.** Receiver operating characteristic (ROC) curves (left) and calibration plots (right) for 3 multivariate models that discriminate between different regions. *Upper row*, Atherosclerotic and hyperplastic versus normal-appearing regions. *Center row*, Thin versus normal-appearing regions. *Lower row*, Atherosclerotic and hyperplastic versus thin regions.